CISC 7332X T6 Some Foundation of Data Communication

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Outline

- Concept of Fourier analysis
- Bandwidth and bandwidth-limited signals
- Maximum data rate of a noiseless channel
- Maximum data rate of a noisy channel
- Wave length and propagation speed

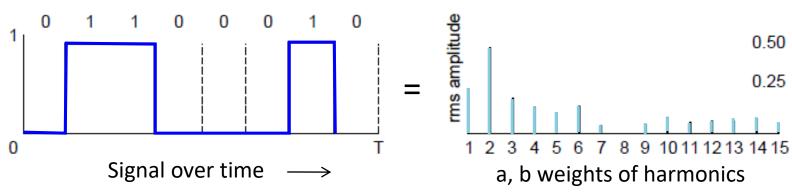
Theoretical Basis for Data Communication

- Communication rates have fundamental limits
 - Fourier analysis
 - Bandwidth-limited signals
 - Maximum data rate of a channel

Fourier Analysis

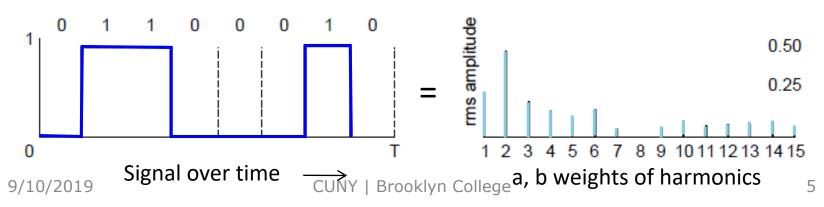
 A time-varying signal can be equivalently represented as a series of frequency components (harmonics)

$$g(t) = \frac{1}{2}c + \sum_{n=1}^{\infty} a_n \sin(2\pi n f t) + \sum_{n=1}^{\infty} b_n \cos(2\pi n f t)$$

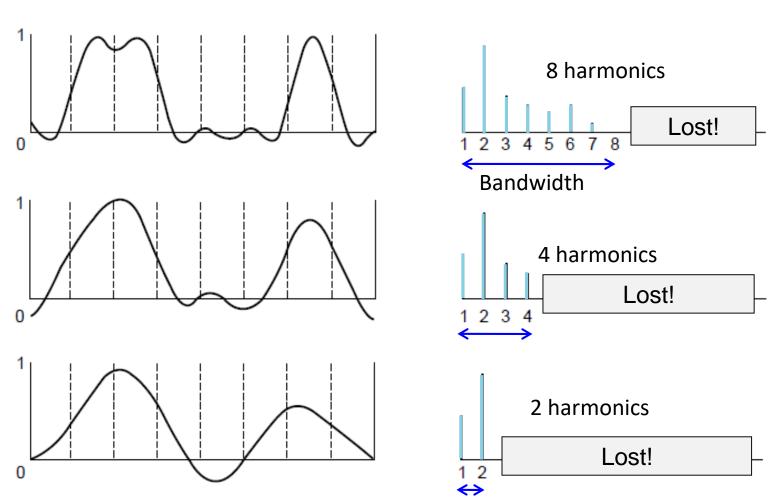


Bandwidth-Limited Signals

- Bandwidth
 - The width of the frequency range transmitted without being strongly attenuated is called the bandwidth
- Having less bandwidth (harmonics) degrades the signal



Bandwidth-Limited Signals



Maximum Data Rate of a Channel

- Noiseless channel
- Noisy channel

Maximum Data Rate of Noiseless Channel

 Nyquist's theorem relates the data rate to the bandwidth (B) and number of signal levels (V):

Max. data rate = $2B \log_2 V$ bits/sec

Example: A Noiseless Channel

- How much is the maximum data rate when transmitting signals of 2-levels over a noiseless 3-KHz channel?
 - which means
 - B = 3 kHz = 3000 Hz
 - V = 2

Max. data rate

- = 2B log₂V bits/sec
- $= 2 \times 3000 \times \log_2 2$
- = 6000 bits / sec

Maximum Data Rate of Noisy Channel

 Shannon's theorem relates the data rate to the bandwidth (B) and signal strength (S) relative to the noise (N):

Max. data rate = $B log_2(1 + S/N)$ bits/sec

How fast signal How many levels can change can be seen

Signal-to-Noise Ratio

- S/N: the signal-to-noise ratio
- Often measured in log-scale, i.e., in decibels (dB)
 - 1 dB = 1 decibel = 1 deci-Bel = 1/10 Bels

SNR in dB =
$$10 \log_{10} S/N dB$$

Example: an ADSL Channel

 Asymmetric Digital Subscriber Line (ADSL) provides Internet access over ordinary telephone lines. Consider an ADSL channel with the bandwidth of 1 Mhz. The SNR depends strongly on the distance of the home from the telephone exchange, and an SNR of ~40dB for short lines of 1 or 2 km is very good. How much is the maximum date rate?

Example: an ADSL Channel

The ADSL channel

- $B = 1 Mhz = 10^6 Hz$
- SNR = 40 dB

Estimate S/N

- $10 \log_{10} (S/N) = 40$
- $S/N = 10^4 = 16$

Max. data rate

- = $B \log_2(1 + S/N)$ bits/sec
- $= 10^6 \times \log_2(1+10^4)$
- $\approx 10^6 \times 13.29$ bits/sec = 13.29 Mbps

In-Class Exercise C05b-1

Television channels are 6 MHz wide. Answer the questions

- 1) How many bits/sec can be sent if 4level digital signals are used? Assume a noiseless channel
- 2) Assume that it is a noisy channel with a SNR 30 dB. How many bits/sec can be sent?

In-Class Exercise C05b-2

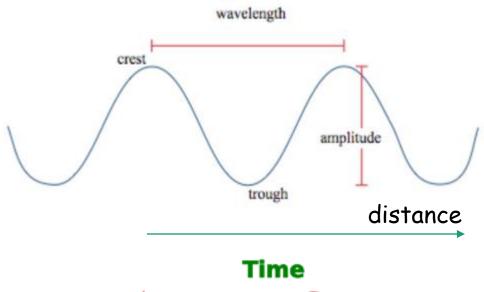
Television channels are 6 MHz wide. Answer the questions

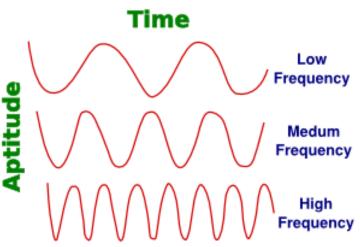
- 1) Assume a noiseless channel. What is the minimum levels of the digital signals is necessary to reach data rate 5 Mbps?
- 2) Assume that it is a noisy channel and you wish to reach a maximum date rate of 5 Mbps. What signal-to-noise ratio is needed? In dB?

Signal and Wave

- Wave length (λ)
- Frequency (f)
- Wave speed (v)

 $v = \lambda f$





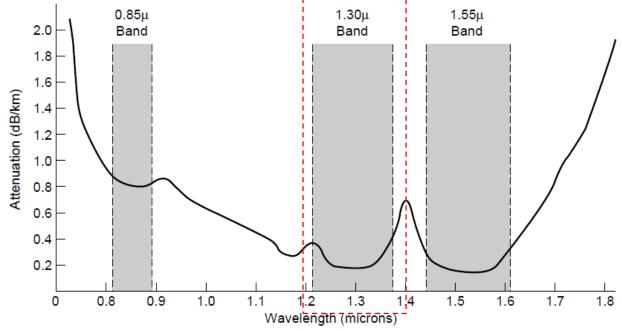
Example: Light in Vacuum

- Consider a visible light of 500 THz traveling in vacuum. How much is the wave length?
- Wave speed
 - v = speed of light in vacuum = c ≈ 3 x 10⁸ meter/sec
 - $f = 500 \text{ THz} = 500 \cdot 10^{12} \text{ Hz} = 500 \cdot 10^{12} \text{ sec}^{-1}$
 - $\lambda = v / f = 3 \times 10^8 / (500 \cdot 10^{12})$
 - $= 6 \cdot 10^{-7} \text{ meters}$
 - $= 600 \cdot 10^{-9}$ meters
 - = 600 nanometers

Example: Bandwidth of a Fiber

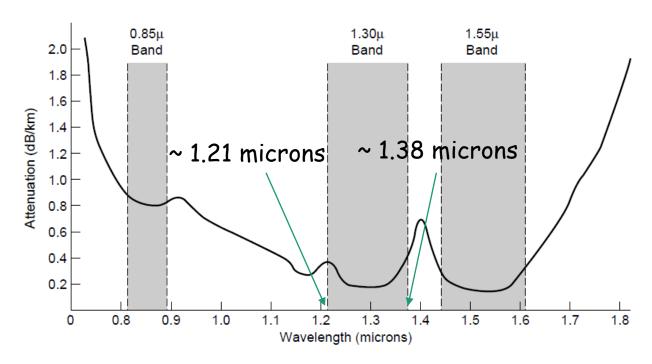
 Consider the 1.30-micron (micro-meter) band in the figure. With a reasonable signal-to-noise ratio of 10 dB, how much is the maximum data





Example: Bandwidth of a Fiber

 Read from the graph, estimate the bandwidth



Example: Bandwidth of a Fiber

Approximately,

$$\begin{array}{l} v=c\approx 3\times 10^8 \; \text{meter/sec} \\ f_{high}=v \: / \: \lambda_{low}\approx 3\times 10^8 \: / \: (1.21\times 10^{-6})\approx 2.48\times 10^{14} \; \text{Hz} \\ f_{low}=v \: / \: \lambda_{high}\approx 3\times 10^8 \: / \: (1.38\times 10^{-6})\approx 2.17\times 10^{14} \; \text{Hz} \\ B\approx (2.48-2.17)\times 10^{14}=0.31\times 10^{14} \; \text{Hz} \end{array}$$
 Since 10 log $_{10}$ S/N = 10 dB, S/N = 10

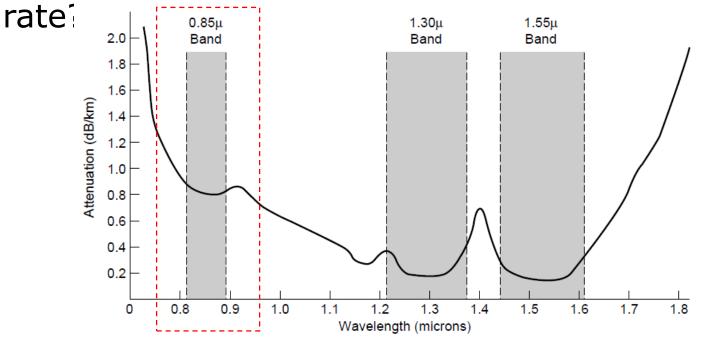
Then

Max. data rate = B
$$\log_2(1 + S/N)$$

 $\approx 0.31 \times 10^{14} \times \log_2(1 + 10) = 0.107 \times 10^{15}$ bits/sec
= 107×10^{12} bits/sec = 107 Tbps

In-Class Exercise C05b-3

 Consider the 0.85-micron (micro-meter) band in the figure. With a reasonable signal-to-noise ratio of 10 dB, how much is the maximum data



Questions?

- Concept of Fourier analysis
- Bandwidth and bandwidth-limited signals
- Maximum data rate of a noiseless channel
- Maximum data rate of a noisy channel
- Relationship among wavelength, frequency, and wave speed
- Exercises and assignments?